# NAG Fortran Library Routine Document F08CKF (DORMRO)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

## 1 Purpose

F08CKF (DORMRQ) multiplies a general real m by n matrix C by the real orthogonal matrix Q from an RQ factorization computed by F08CHF (DGERQF).

## 2 Specification

```
SUBROUTINE FO8CKF (SIDE, TRANS, M, N, K, A, LDA, TAU, C, LDC, WORK,

LWORK, INFO)

INTEGER

M, N, K, LDA, LDC, LWORK, INFO

double precision

CHARACTER*1

SIDE, TRANS
```

The routine may be called by its LAPACK name dormrq.

## 3 Description

F08CKF (DORMRQ) is intended to be used following a call to F08CHF (DGERQF), which performs an RQ factorization of a real matrix A and represents the orthogonal matrix Q as a product of elementary reflectors.

This routine may be used to form one of the matrix products

$$QC$$
,  $Q^{\mathrm{T}}C$ ,  $CQ$ ,  $CQ^{\mathrm{T}}$ ,

overwriting the result on C, which may be any real rectangular m by n matrix.

A common application of this routine is in solving underdetermined linear least squares problems, as described in the F08 Chapter Introduction, and illustrated in Section 9 of the document for F08CHF (DGERQF).

#### 4 References

Anderson E, Bai Z, Bischof C, Blackford S, Demmel J, Dongarra J J, Du Croz J J, Greenbaum A, Hammarling S, McKenney A and Sorensen D (1999) *LAPACK Users' Guide* (3rd Edition) SIAM, Philadelphia URL: http://www.netlib.org/lapack/lug

Golub G H and Van Loan C F (1996) *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

## 5 Parameters

1: SIDE – CHARACTER\*1

On entry: indicates how 
$$Q$$
 or  $Q^{T}$  is to be applied to  $C$ .

SIDE = 'L'

 $Q$  or  $Q^{T}$  is applied to  $C$  from the left.

SIDE = 'R'

 $Q$  or  $Q^{T}$  is applied to  $C$  from the right.

Constraint: SIDE = 'L' or 'R'.

Input

### 2: TRANS - CHARACTER\*1

Input

On entry: indicates whether Q or  $Q^{T}$  is to be applied to C.

TRANS = 'N'

Q is applied to C.

TRANS = 'T'

 $Q^{\mathrm{T}}$  is applied to C.

Constraint: TRANS = 'N' or 'T'.

#### 3: M - INTEGER

Input

On entry: m, the number of rows of the matrix C.

Constraint:  $M \ge 0$ .

#### 4: N - INTEGER

Input

On entry: n, the number of columns of the matrix C.

Constraint:  $N \geq 0$ .

#### 5: K – INTEGER

Input

On entry: k, the number of elementary reflectors whose product defines the matrix Q.

Constraints:

$$\begin{array}{l} \text{if SIDE} = \text{'L'}, \; M \geq K \geq 0; \\ \text{if SIDE} = \text{'R'}, \; N \geq K \geq 0. \end{array}$$

## 6: A(LDA,\*) – *double precision* array

Input/Output

**Note**: the second dimension of the array A must be at least max(1, M) if SIDE = 'L' and at least max(1, N) if SIDE = 'R'.

On entry: the *i*th row of A must contain the vector which defines the elementary reflector  $H_i$ , for i = 1, 2, ..., k, as returned by F08CHF (DGERQF).

On exit: is modified by F08CKF (DORMRQ) but restored on exit.

#### 7: LDA – INTEGER

Input

On entry: the first dimension of the array A as declared in the (sub)program from which F08CKF (DORMRQ) is called.

Constraint: LDA  $\geq \max(1, K)$ .

#### 8: TAU(\*) – *double precision* array

Input

**Note**: the dimension of the array TAU must be at least max(1, K).

On entry: TAU(i) must contain the scalar factor of the elementary reflector  $H_i$ , as returned by F08CHF (DGERQF).

### 9: C(LDC,\*) – *double precision* array

Input/Output

**Note**: the second dimension of the array C must be at least max(1, N).

On entry: the m by n matrix C.

On exit: is overwritten by QC or  $Q^{T}C$  or CQ or  $CQ^{T}$  as specified by SIDE and TRANS.

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10: LDC – INTEGER Input

On entry: the first dimension of the array C as declared in the (sub)program from which F08CKF (DORMRQ) is called.

*Constraint*: LDC  $\geq \max(1, M)$ .

11: WORK(\*) – *double precision* array

Workspace

**Note**: the dimension of the array WORK must be at least max(1, LWORK).

On exit: if INFO = 0, WORK(1) contains the minimum value of LWORK required for optimal performance.

12: LWORK – INTEGER

Input

On entry: the dimension of the array WORK as declared in the (sub)program from which F08CKF (DORMRQ) is called.

If LWORK = -1, a workspace query is assumed; the routine only calculates the optimal size of the WORK array, returns this value as the first entry of the WORK array, and no error message related to LWORK is issued.

Suggested value: for optimal performance, LWORK  $\geq$  N  $\times$  nb if SIDE = 'L' and at least M  $\times$  nb if SIDE = 'R', where nb is the optimal **block size**.

Constraints:

```
if SIDE = 'L', LWORK \geq max(1, N) or LWORK = -1; if SIDE = 'R', LWORK \geq max(1, M) or LWORK = -1.
```

13: INFO – INTEGER

Output

On exit: INFO = 0 unless the routine detects an error (see Section 6).

## 6 Error Indicators and Warnings

Errors or warnings detected by the routine:

INFO < 0

If INFO = -i, the *i*th parameter had an illegal value. An explanatory message is output, and execution of the program is terminated.

## 7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$||E||_2 = O\epsilon ||C||_2$$

where  $\epsilon$  is the *machine precision*.

#### **8 Further Comments**

The total number of floating point operations is approximately 2nk(2m-k) if SIDE = 'L' and 2mk(2n-k) if SIDE = 'R'.

The complex analogue of this routine is F08CXF (ZUNMRQ).

## 9 Example

See Section 9 of the document for F08CHF (DGERQF).